

# SLAM IV

## Boolean Model Checking

Verification & Testing  
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# SLAM thus far

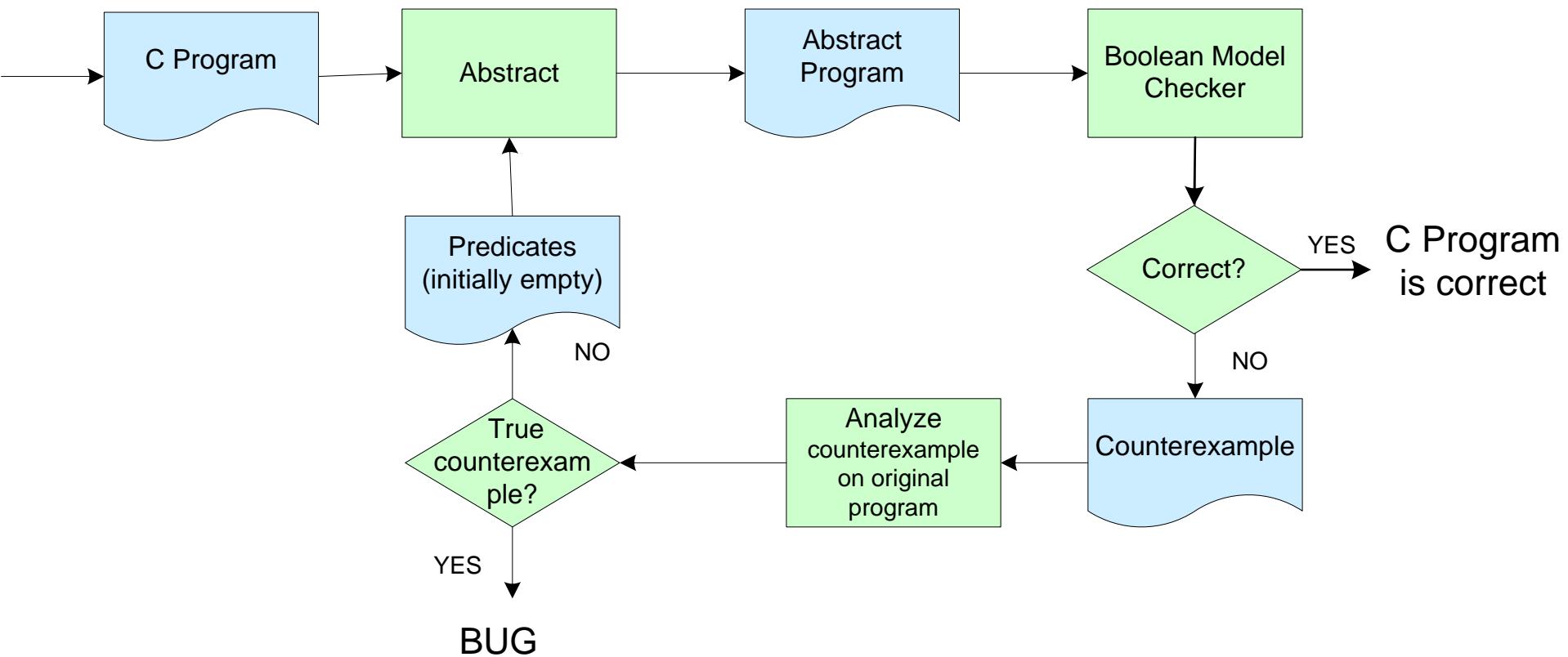
Automatic model checking of C programs

Abstraction/Refinement loop

- Predicate abstractions
- Initial abstraction: no predicates, only control flow
- When abstract program correct, so is concrete program
- When bug found in abstract program, check on concrete program
- If bug is real, stop.
- If bug is not real, add predicates to prove impossibility of path, create new abstraction, and redo

This week: Model checking Boolean Programs

# The Approach



# Model Checking Boolean Programs

**Question:** can Boolean program make nondeterministic decisions such that assertion is violated?

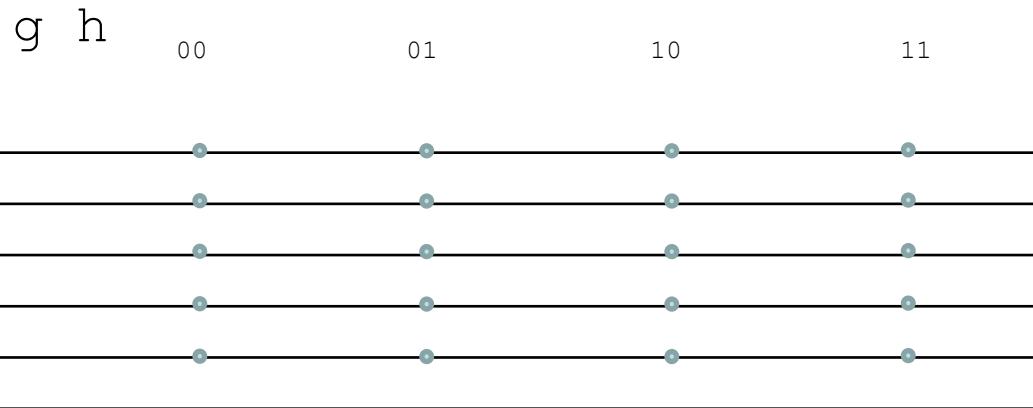
```
01. decl g
02. main() {
03.     decl h;
04.     h = !g;
05.     A(g,h);
06.     A(g,h);
07.
assert(!g);
08. }
```

```
09. A(a1,a2) {
10.     if(a1) {
11.
12.
A(a2,a1);
13.     }else{
14.
15.         g =
a2;
16.     }
17. }
```

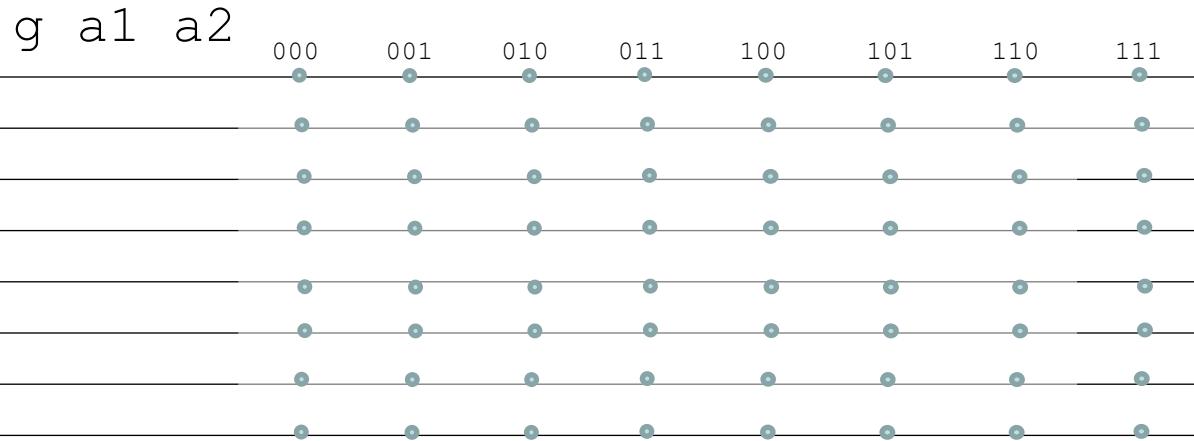
# Example

# Example

```
01. decl g
02. main(){
03.   decl h;
04.   h = !g;
05.   A(g,h);
06.   A(g,h);
07.   assert(!g);
08. }
```



```
09. A(a1,a2){
10.   if(a1){
11.
12.     A(a2,a1);
13.   }else{
14.
15.     g = a2;
16.   }
17. }
```



# Some Definitions

A *valuation* gives a value to a set of variables.

The *visible variables* are the global variables plus the local variables that are in scope

For function calls,

- The *caller* is the calling function
- The *callee* is the called function

We add *points* to every line

- A point is labeled with a valuation of the visible variables (the valuation after execution of the line)
- A point is marked “done” or “not done”

We add arrows

- blue arrows for control flow
- green arrows for function calls
- black arrows for returns

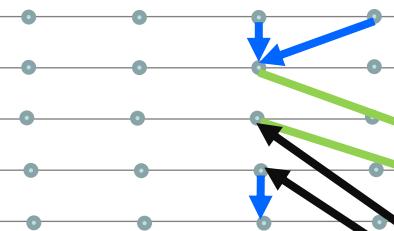
# Example

g h

```

01. decl g
02. main() {
03.   decl h;
04.   h = !g;
05.   A(g,h);
06.   A(g,h);
07.   assert(!g);
08. }
```

00      01      10      11

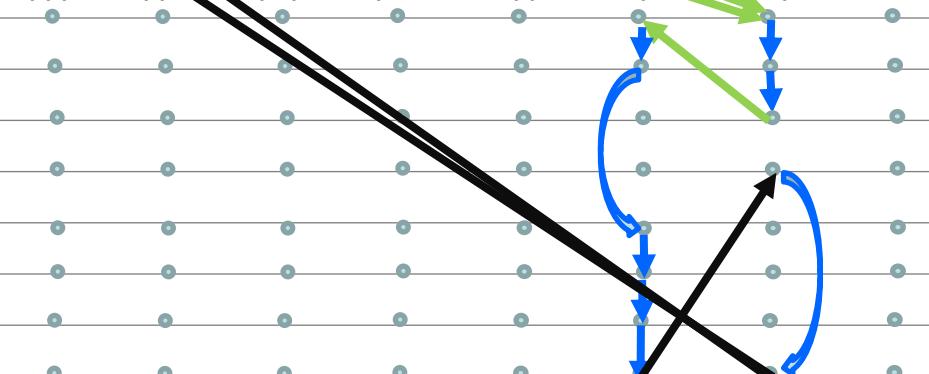


g a1 a2

```

09. A(a1,a2) {
10.   if(a1) {
11.
12.     A(a2,a1);
13.   }else{
14.
15.     g = a2;
16.   }
17. }
```

000      001      010      011      100      101      110      111



# Example

```
01. decl g
02. main() {
03.     decl h;
04.     h = !g;
05.     A(g,h);
06.     A(g,h);
07.     assert(!g);
08. }
09. A(a1,a2) {
10.     if(a1) {
11.
12.         A(a2,a1);
13.     }else{
14.
15.         g = a2;
16.     }
17. }
```

Bug:

```
03. g=1, h=0
04. g=1, h=0
09. g=1, a1=1, a2=0
11. g=1, a1=1, a2=0
09. g=1, a1=0, a2=1
14. g=1, a1=0, a2=1
15. g=1, a1=0, a2=1
12. g=1, a1=1, a2=0
16. g=1, a1=1, a2=0
05. g=1, h=0
09. g=1, a1=1, a2=0
11. g=1, a1=1, a2=0
09. g=1, a1=0, a2=1
14. g=1, a1=0, a2=1
15. g=1, a1=0, a2=1
12. g=1, a1=1, a2=0
16. g=1, a1=1, a2=0
06. g=1, h=0
07. assert(false) !
```

# Example

```
01. decl g
02. main() {
03.     decl h;
04.     h = !g;
05.     A(g,h);
06.     A(g,h);
07.     assert(!g);
08. }

09. A(a1,a2) {
10.     if(a1) {
11.
12.         A(a2,a1);
13.     }else{
14.
15.         g = a2;
16.     }
17. }
```

Note:

Example is deterministic (no \*)

Example has an infinite loop.

- This is not a bug
- The model checker should still finish

# Model Checking

We perform forward analysis and build graph. Nodes: combination of line number and valuation of variables. Arrows: **blue** (normal execution) and **green** (function calls).

At beginning of main, add point for every valuation

For every point p not marked *done*:

- If next statement is
  - **assignment**: compute new valuations, add point q to next line, label with each valuation. (Nondeterminism can cause multiple valuations)
  - **if**: Add point q with same valuation to beginning of then or else branch. (or both if condition is \*)
  - **while statement**: Like if
  - **end of function f**: For all p' with **green arrow** to the start of f and path of **blue arrows** from start of f to p (calls to f that end in p), compute new valuation of caller and add point q with this valuation.
  - **assert**: Condition false? Bug! Otherwise, create q with same valuation after assert.
- Mark p done. If not at end of function, add blue arrow from p to q
- If next statement is **function call**: compute valuation local to function, add point q to start of callee, add **green arrow** from p to q

All points marked done and no bug found? program is correct!

# Function Calls

Function calls are call-by-value (like in C)

When calling a function,

- Value of globals in callee = value of globals in caller before call
- Value of formal parameters in callee = value of actual parameters in caller before call

When returning

- Value of globals in caller after call = value of globals in callee at end of function
- Value of locals in caller after call = value of locals in caller before call

# Example, Notes

For a given function and valuation there may be

- No call with that valuation: ignored
- A call but no returns: infinite loop
- A call and one return: deterministic
- A call and multiple returns.
- The last case happens if there is nondeterminism in the function. Every return is propagated to caller. Try replacing `if(a1)` by `if(*)` in example.

There may be multiple callers for every valuation

We avoid infinite loops by keeping track of valuations we have seen before.

# Another Example: nondeterminism

```
01. decl g
02. main() {
03.   A(g,g)
04.   assert(g);
05. }
06. A(a1,a2) {
07.   if(*) {
08.     g = a1;
09.   } else {
10.     g = !a1
11.   }
13. }
```

# Another Example: nondeterminism

```
01. decl g
02. main() {
03.   A(g,g)
04.   assert(g);
05. }
06. A(a1,a2) {
07.   if(*) {
08.     g = a1;
09.   } else {
10.     g = !a1
11.   }
13. }
```

Note:

Nondeterminism causes two outgoing transitions for each point on line 7 and line 3.

For instance:

- In line 7 with  $(g,a1,a2)=(0,0,0)$ , we can go to line 8 with  $(0,0,0)$  or line 10 with  $(0,0,0)$ .
- In line 3 with  $g = 0$  we can go to line 4 with  $g = 0$  or line 4 with  $g = 1$ .

# Concluding

Model checking a Boolean program

It's simple, just keep track of what you've done