

Model Checking

Lecture:

Roderick Bloem, Bettina Könighofer, Stefan Pranger

Practicals:

Vedad Hadžić, Johannes Haring

IAIK

Today

Administrative
Motivation

737 Max



“The people who wrote the code for the original MCAS system were obviously terribly far out of their league and did not know it”.

346 deaths

IAIK Deductive Verification?

```
r = false;
i = 0;
while(i != n) {

    if(a[i] == x) {

        r = true;
    } else {

    }

    i = i + 1;
}
```

TALK Deductive Verification?

```
{false == false} ↔ {true}
r = false;
{r == (Vj=0-1 a[j] == x)} ↔ {r == false}
i = 0;
{r == (Vj=0i-1 a[j] == x)}
while(i != n) {
  {(r == (Vj=0i-1 a[j] == x)) ∧ i != n}
  {r == (Vj=0i-1 a[j] == x)}
  if(a[i] == x) {
    {(r == (Vj=0i-1 a[j] == x)) ∧ a[i] == x}
    {(true == (Vj=0i a[j] == x)) ∧ a[i] == x} ↔ {true ∧ a[i] == x} ↔ {a[i] == x}
    r = true;
    {r == (Vj=0i a[j] == x)}
  } else {
    {(r == (Vj=0i a[j] == x)) ∧ a[i] != x} ↔ {(r == (Vj=0i-1 a[j] == x)) ∧ a[i] != x}
  }
  {r == (Vj=0i a[j] == x)}
  i = i + 1;
  {r == (Vj=0i-1 a[j] == x)}
}
{r == (Vj=0n-1 a[j] == x) ∧ i == n} ↔ {r == (Vj=0i-1 a[j] == x) ∧ i == n}
{r == (Vj=0n-1 a[j] == x)}
```

- (Manual) Proofs
- No diagnostics
- Full specifications
- Concurrency is hard

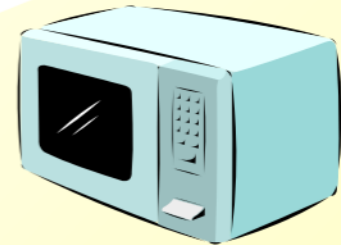
(But: things have gotten better!)

Automatic Verification!

- Program = state machine = graph
- Bug hunting = efficient graph search
- “Interesting” properties = “complicated” graph searches
 - Need language to express interesting things!
- But how to search a graph efficiently?

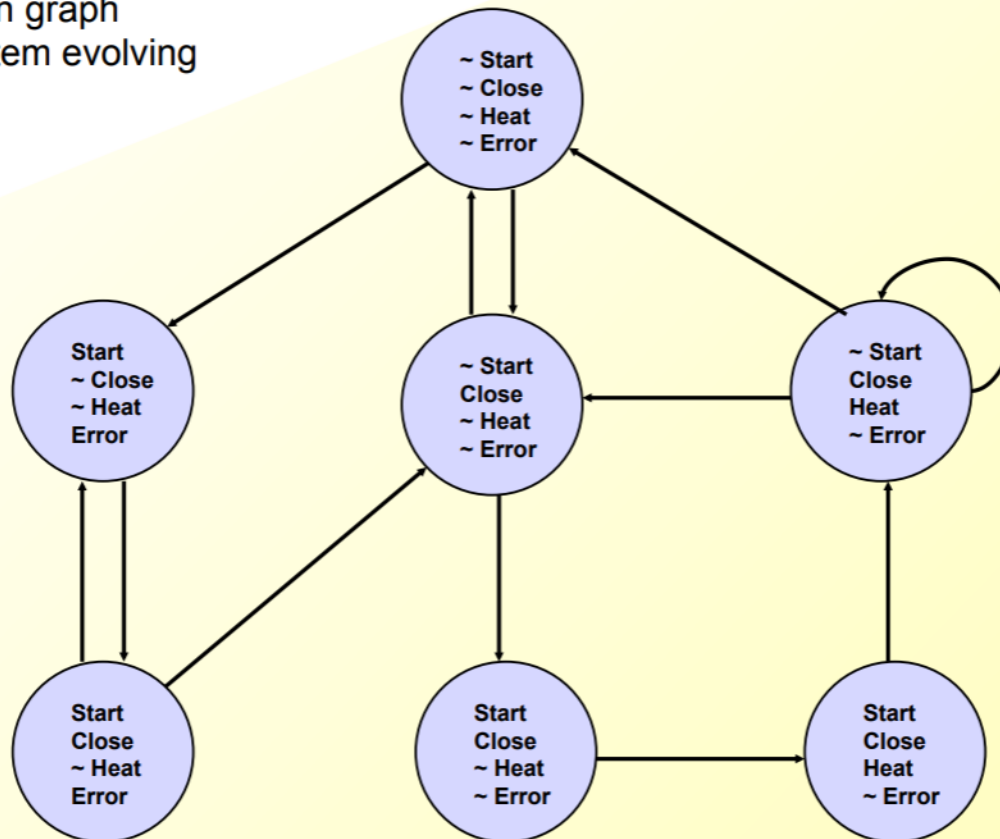
TALK
TALK

Model of computation



Microwave Oven Example

State-transition graph describes system evolving over time.



What properties are interesting?

Slide by Ed Clarke

Efficiency

- 1981: EMC Model checker $\sim 10^4$ states
- 1992 BDDs:

Symbolic Model Checking: 10^{20} States and Beyond*

J. R. BURCH, E. M. CLARKE, AND K. L. McMILLAN

*School of Computer Science, Carnegie Mellon University,
Pittsburgh, Pennsylvania 15213*

AND

D. L. DILL AND L. J. HWANG

Stanford University, Stanford, California 94305

- 1999 SAT:

Symbolic Model Checking without BDDs*

Armin Biere¹, Alessandro Cimatti², Edmund Clarke¹, and Yunshan Zhu¹

Efficiency

1992 Abstraction

Construction of Abstract State Graphs with PVS

Susanne Graf and Hassen Saidi
VERIMAG¹
{graf,saidi}@imag.fr

~1995: Partial Order Reduction

~2000: Software

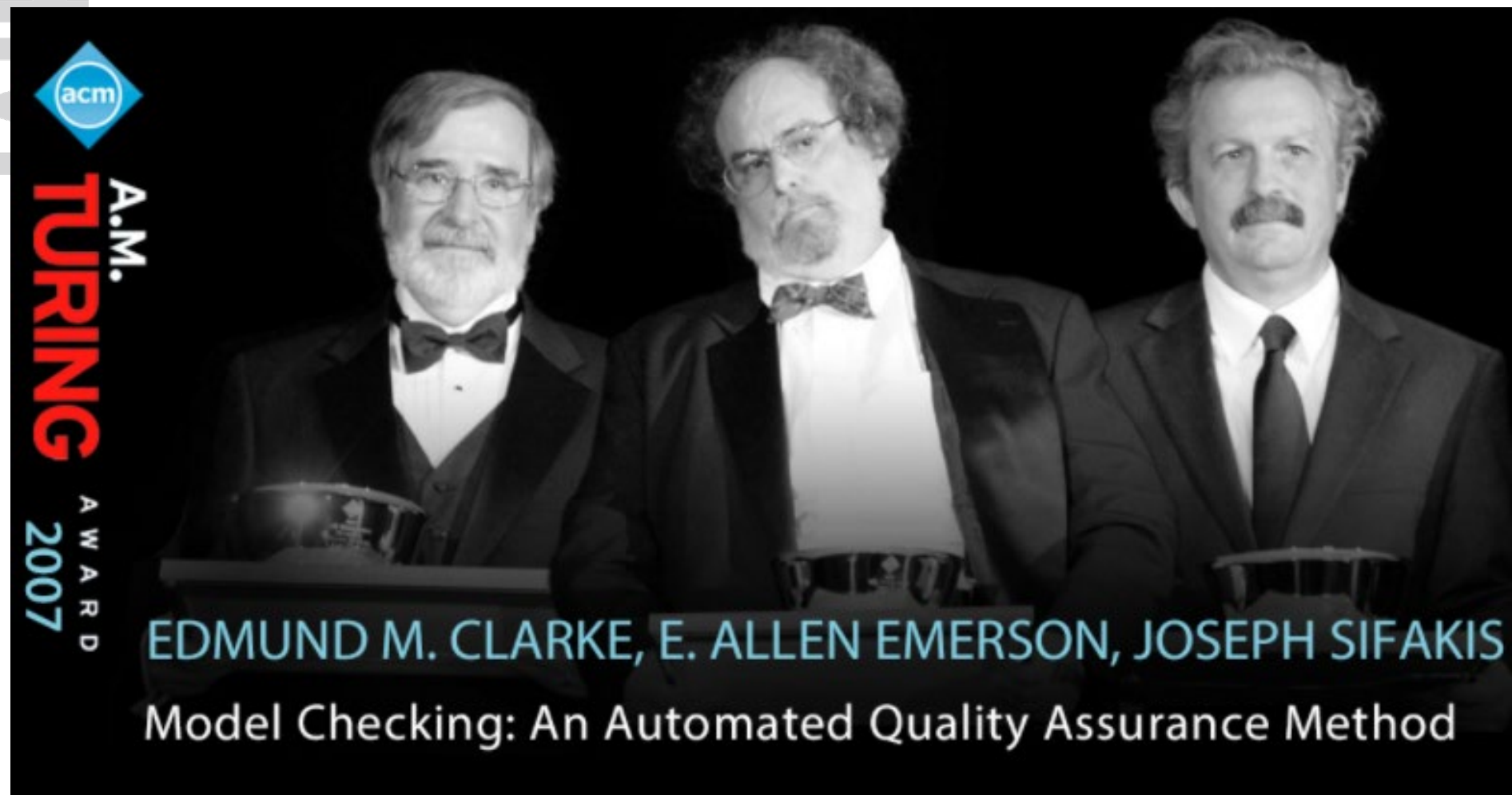
The SLAM Toolkit

Thomas Ball and Sriram K. Rajamani

Microsoft Research
<http://www.research.microsoft.com/slam/>

More than Microwave Ovens?

- Amazon Web Services
 - S3, DynamoDB, EBS, lock manager
 - <https://assets.amazon.science/67/f9/92733d574c11ba1a11bd08bfb8ae/how-amazon-web-services-uses-formal-methods.pdf>
- Facebook
 - Static Analysis <https://research.facebook.com/publications/moving-fast-with-software-verification/>
- Intel
 - Security https://community.cadence.com/cadence_blogs_8/b/breakfast-bytes/posts/formally-verifying-processor-security
- Microsoft
 - Device drivers
 - Smart contracts
 - Z3
- Cadence & Synopsys
 - Jasper Formal Verification, VC Formal



acm
A.M.
TURING
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2007

EDMUND M. CLARKE, E. ALLEN EMERSON, JOSEPH SIFAKIS
Model Checking: An Automated Quality Assurance Method

Material & Communications

OLD FASHIONED, PHYSICAL LECTURE!

Lecture: Monday 9-10:30, IFEG042 (Seminar Room IAIK)

Practicals: Right after, only if there is something to discuss

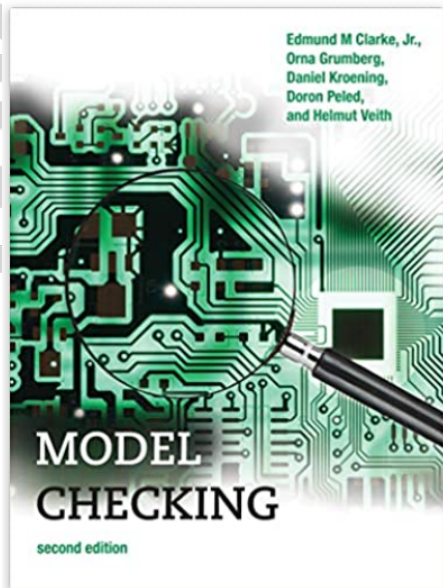
Question Hours: Monday after class.

Webpage: <https://www.iaik.tugraz.at/course/model-checking-705080-sommersemester-2024/>

Discord: <https://discord.gg/FDcxjR728N>, Channel MC (robot)

Email: bettina.koenighofer@iaik.tugraz.at,
roderick.bloem@iaik.tugraz.at, stefan.pranger@iaik.tugraz.at
johannes.haring@iaik.tugraz.at, vedad.hadzic@iaik.tugraz.at

IAIK The Book



Model Checking, second edition (Cyber Physical Systems Series) Gebundene Ausgabe – 4. Dezember 2018

Englisch Ausgabe | von Edmund M. Clarke Jr. (Autor), & 4 mehr

★★★★★ 2 Sternebewertungen

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GRATIS Lieferung: **Montag, 8. Mär.** Siehe Details.

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Abhängig von der Lieferadresse
kann die USt. an der Kasse
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**Nur noch 1 auf Lager (mehr
ist unterwegs).**

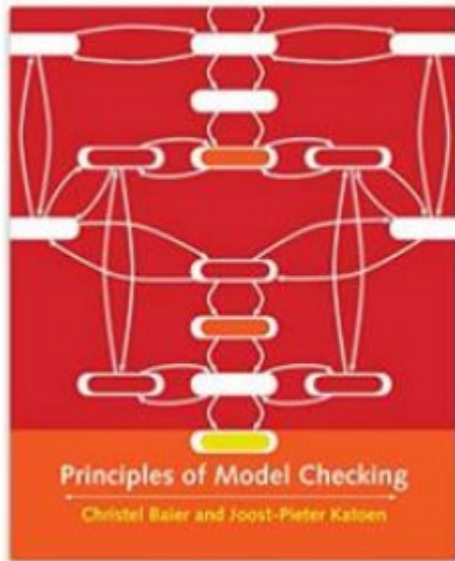
Verfügbar als **Kindle eBook**. Kindle
eBooks können mit der kostenlosen
Kindle-App auf allen Geräten
gelesen werden.

Verkauf und Versand durch Amazon.

Menge:

Clarke, Grumberg, Kroening, Peled, Veith, *Model Checking*, MIT Press 2018
(This is the second edition. The first has a shorter author list.)

IAIK The Book



Principles of Model Checking (Mit Press) Gebundene Ausgabe – Illustriert, 25.

April 2008

Englisch Ausgabe | von Christel Baier ~ (Autor), Joost-Pieter Katoen (Autor)

★★★★☆ 16 Sternebewertungen

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Möchten Sie Ihre Elektro- und Elektronikgeräte kostenlos recyceln? [Mehr erfahren](#)

Baier, Katoen. *Principles of Model Checking*, MIT Press, 2008

Another good book:

Clarke, Henzinger, Veith, Bloem, *Handbook of Model Checking*, Springer 2018

How to get a grade?

Lecture: Two options

1. Do an exam, **or**
2. Participate in class, and do weekly homework. Course grade = homework grade

(Not happy with homework grade? Take exam!)

Details:

- Miss at most 2 classes
- Skip at most 2 homeworks

Practical:

- Individual work
- Three assignments with point distribution 30/40/30
- Final interviews

Homework

- Weekly homework
 - uploaded just before the lecture
 - deadline start of the next lecture
- **Individually** or **groups of two**.
 - You can do each homework with a different group.
- Submission
 - In TeachCenter
 - If handwritten, use **clear writing** and a good scan
- Marks
 - available within 1 week of submission deadline at <https://cloud.tugraz.at/index.php/s/zeEgt8ptcRQCXEW>
 - Final mark = **average of all homework** (even those you do not hand in).
 - You can skip homework **at most 2** weeks.
- Questions
 - email: filip.cano@iaik.tugraz.at
 - I also actively answer questions in the discord channel

Lecture Schedule

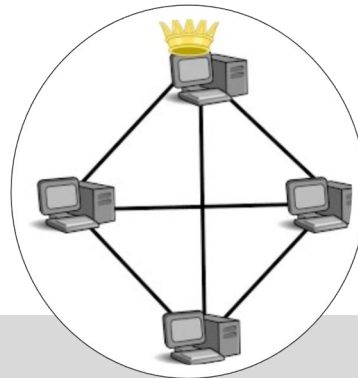
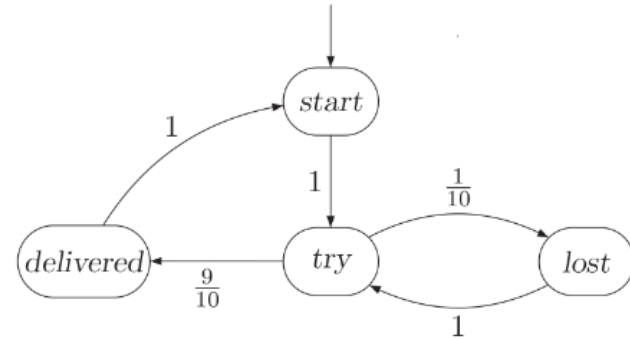
Date	Topic	Lecturer
11.03.2024	Intro	Roderick
18.03.2024	SAT-Based Model Checking (BMC, k-induction) – Chapter 10	Roderick
08.04.2024	SAT-Based Model Checking (interpolation) -Chapter 10	Roderick
15.04.2024	SAT-Based Model Checking (PDR) – Chapter 10	Roderick
22.04.2024	Temporal Logic – Chapter 4	Bettina
29.04.2024	CTL Model Checking – Chapter 5	Bettina
06.05.2024	CTL Model Checking – Chapter 5	Bettina
13.05.2024	LTL Model Checking -Chapter 7	Bettina
27.05.2024	Probabilistic Model Checking – Chapter 10 – PRISM & Reachability in Markov Chains	Stefan
03.06.2024	Probabilistic Model Checking – Chapter 10 – PCTL and MDPs	Stefan
10.06.2024	Probabilistic Model Checking – Tempest and Shielded Reinforcement Learning	Stefan
17.06.2024	Reserved slot	---

Practicals Schedule

Date	Type	Topic	Lecturer
11.03.2024	Lecture	Intro	Roderick
18.03.2024	Handout	Warmup Exercise	Vedad
08.04.2024	Tutorial	Introduction to Z3	Vedad
15.04.2024	Handout	BMC Exercise	Vedad
21.04.2024	Deadline	Warmup Deadline	—
22.04.2024	Tutorial	Hardware and Verilog	Vedad
29.04.2024	Question Hour	Question Hour BMC	Vedad
06.05.2024	Handout	K-Induction Exercise	Vedad
12.05.2024	Deadline	BMC Deadline	—
13.05.2024	Question Hour	Question Hour K-Induction	Vedad
27.05.2024	Question Hour	Question Hour K-Induction	Vedad
02.06.2024	Deadline	K-Induction Deadline	—

Why do we need Probabilities?

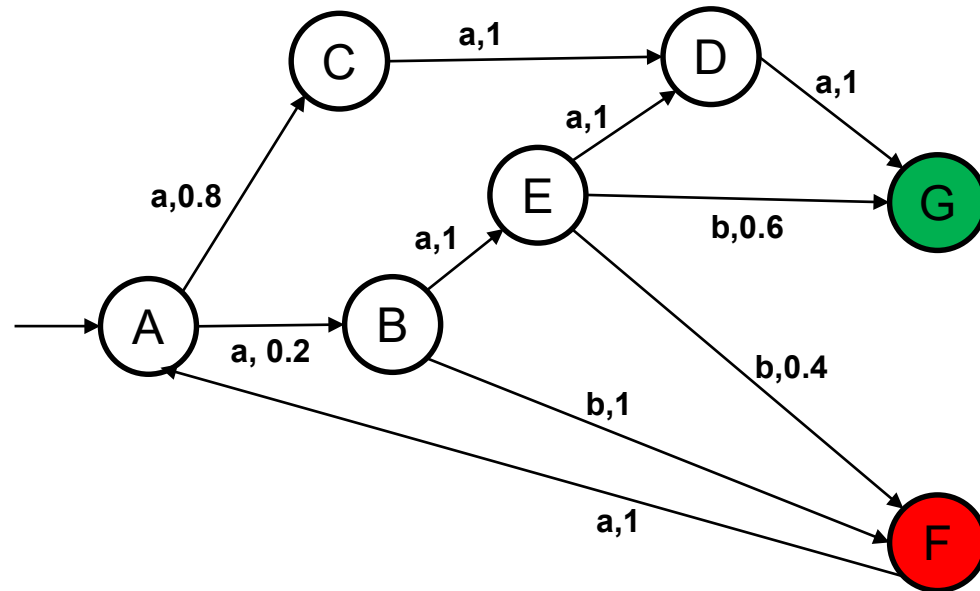
- Analysis of Reliability
 - Probability of Failure,
 - Quantify Message Loss,
 - Quantify Arrival Times, ...
- Models of Safety-Critical Systems,
 - Modelling Unknowns,
 - Modelling Faults, ...
- Analysis of Randomized Algorithms,



...

Probabilistic Model Checking

- Extend Models with Probabilistic Transitions
- "Markov Models"

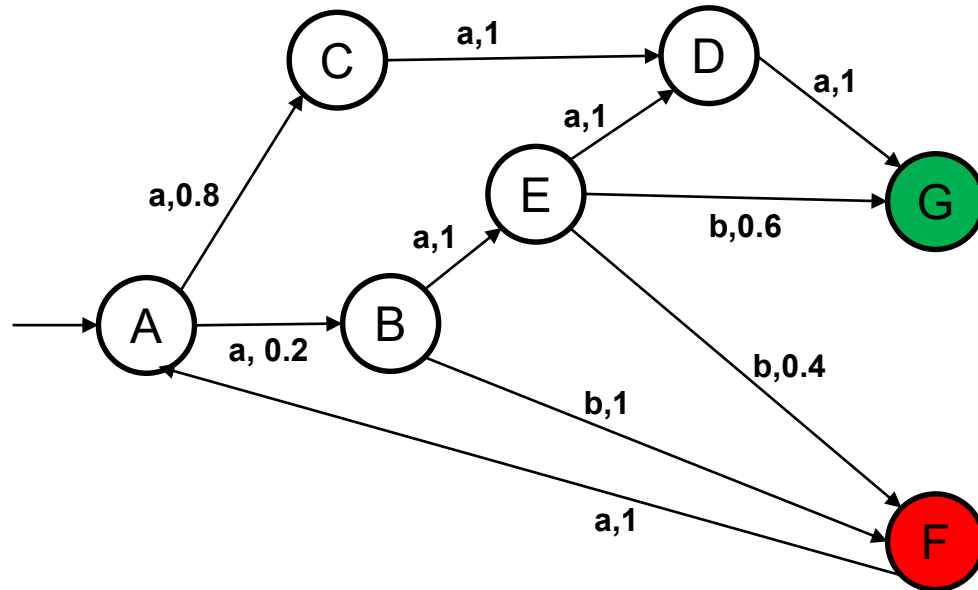


Probabilistic Model Checking

- Formalism to quantify Probabilities

$$P_{\leq 0.95} (F \rightarrow \text{true } U^{<9} G)$$

Is the probability of delivering a message within 9 steps after encountering a failure greater or equal 0.95?

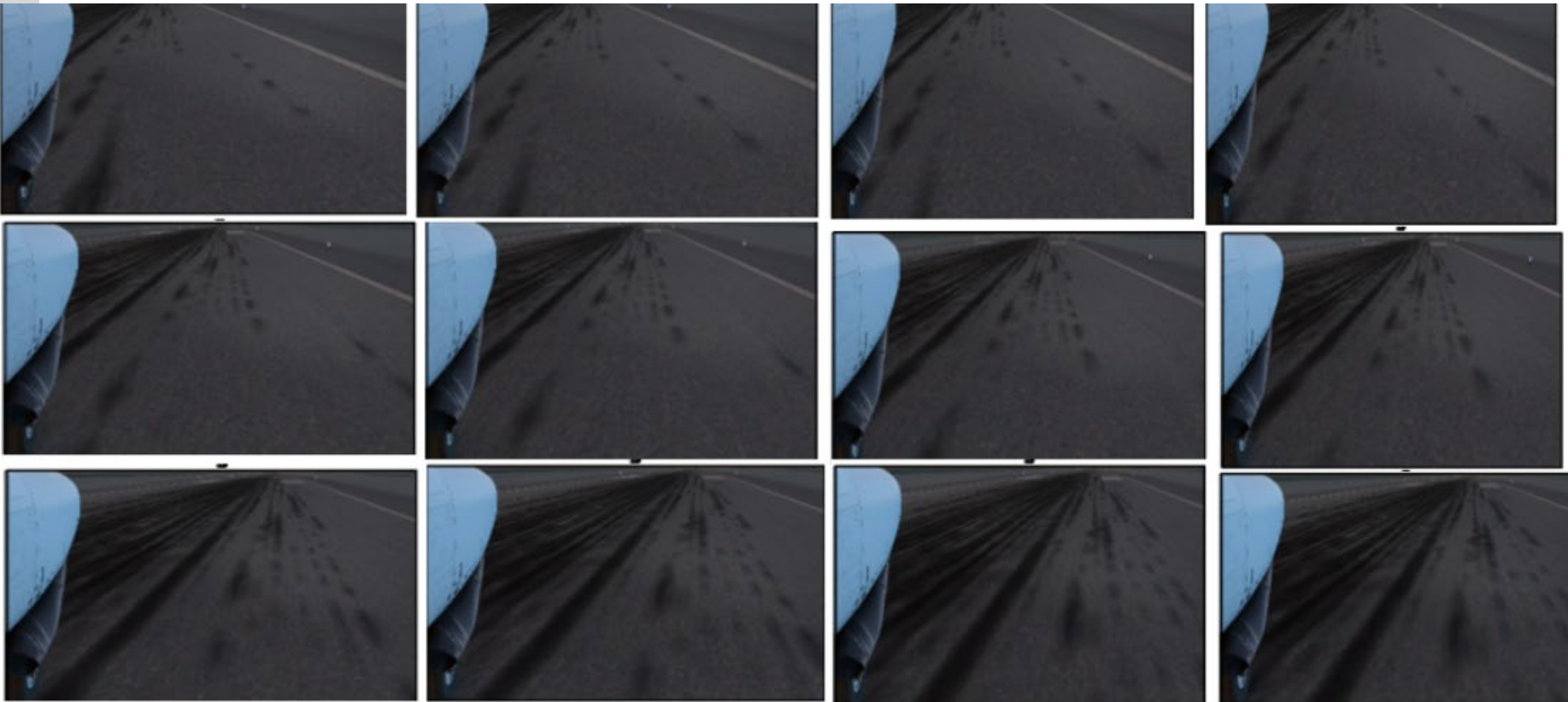


A Probabilistic Model

- Model containing:
 - System Dynamics
 - Controller Decisions
- $P_{<0.01} (F \text{ dist}(\text{airplane}, \text{centerline}) < 200) ?$



TALK Perception is hard to model!

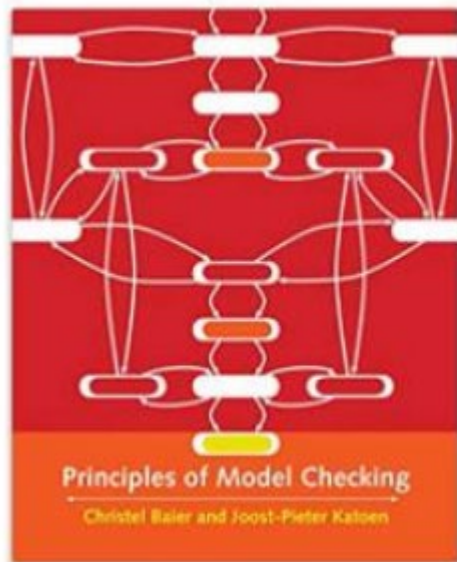


Book

- Different Markovian Models,
 - *and how to compute probabilities of events.*
- Modelling Language,
 - *and how to use a probabilistic model checker, and*
- pMC in practice.

storm & tempest

The Book



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